

Derivation of the Minimum Depth Formula for Constrained Posts

Variable

P is the horizontal wind force

Units

lbs

h is the overall fence height

ft

$\frac{1}{2}h$ is the force application height **for fencing**

ft

b is the diameter of the footing

ft

S_3 is the lateral soil pressure at Footing Depth, D

psf

Q is the resultant of the lateral soil pressure

lbs

d is the minimum embedment depth

ft

D is the Footing Depth being checked ($D \geq d$ is OK)

ft

$Q = \frac{1}{3} S_3 d b$ (Area of the parabolic spandrel times the post width)

Taking the moment about the point of rotation $P \frac{1}{2}h = Q c$

Replace Q with formula

$$P \frac{1}{2}h = \frac{1}{3} S_3 d b c$$

$c = \frac{3}{4} d$ (Centroidal depth of a side opening parabolic spandrel)

$$P \frac{1}{2}h = \frac{1}{3} S_3 d b \frac{3}{4} d = S_3 b \frac{1}{4} d^2$$

Rearrange the formula to find d

$$d^2 = \frac{P \frac{1}{2}h}{S_3 b \frac{1}{4}}$$

$$d^2 = \frac{4.0 P \frac{1}{2}h}{S_3 b}$$

$$d = \sqrt{\frac{4.0 P \frac{1}{2}h}{S_3 b}}$$

This result is within 3% of the IBC Equation 18-2 **modified for fencing**

$$d = \sqrt{\frac{4.25 P \frac{1}{2}h}{S_3 b}}$$

EP486.1 also uses 4.0 per the above derivation.

It is thought that the IBC formula used 4.25 to make it a little more conservative than the actual derived formula.

